

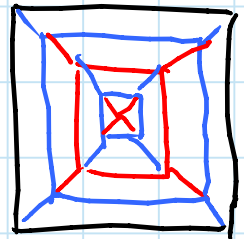
Erik's main research areas:

- computational geometry [6.850]
- geometric folding algorithms [6.849]
- self-assembly
- data structures [6.851]
- graph algorithms [6.889]
- recreational algorithms [SP.268]
- algorithmic sculpture

Geometric folding algorithms: [6.849, videos online]

- design: algorithms to fold any polyhedral surface from a square of paper  
[Demaine, Demaine, Mitchell 2000; Demaine & Tachi 2011]
- bicolor paper  $\Rightarrow$  can 2-color faces
- OPEN: how to best optimize "scale factor"
- e.g. best  $n \times n$  checkerboard folding  
recently improved from  $\sim n/2 \rightarrow \sim n/4$
- foldability: given a crease pattern, can you fold it flat?
- NP-complete in general [Bern & Hayes 1996]
- OPEN:  $m \times n$  map with creases specified as mountain/valley [Edmonds 1997]
- just solved:  $2 \times n$  [Demaine, Liu, Morgan 2011]

- hyperbolic paraboloid [Bauhaus 1929]  
doesn't exist!



[Demaine, Demaine, Hart, Price, Tachi 2009]

- understanding circular creases

- any straight-line graph can be made by  
folding flat & one straight cut

[Demaine, Demaine, Lubiw 1998;

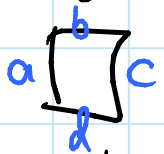
Bern, Demaine, Eppstein, Hayes 1999]

Self-assembly: geometric model of computation

- glue: e.g. DNA strands, each pair has strength

- square tiles with glue on each side

- Brownian motion: tiles/constructions



stick together if  $\sum_i \text{glue strengths} \geq \text{temperature}$

- can build  $n \times n$  square using  $O\left(\frac{\lg n}{\lg \lg n}\right)$  tiles  
[Rothemund & Winfree 2000]

or using  $O(1)$  tiles &  $O(\lg n)$  "stages"

algorithmic steps by the bioengineer

[Demaine, Demaine, Fekete, Ishaque, Rafalin, Schweller, Souvaine 2007]

- can replicate  $\infty$  copies of given unknown  
shape using  $O(1)$  tiles &  $O(1)$  stages

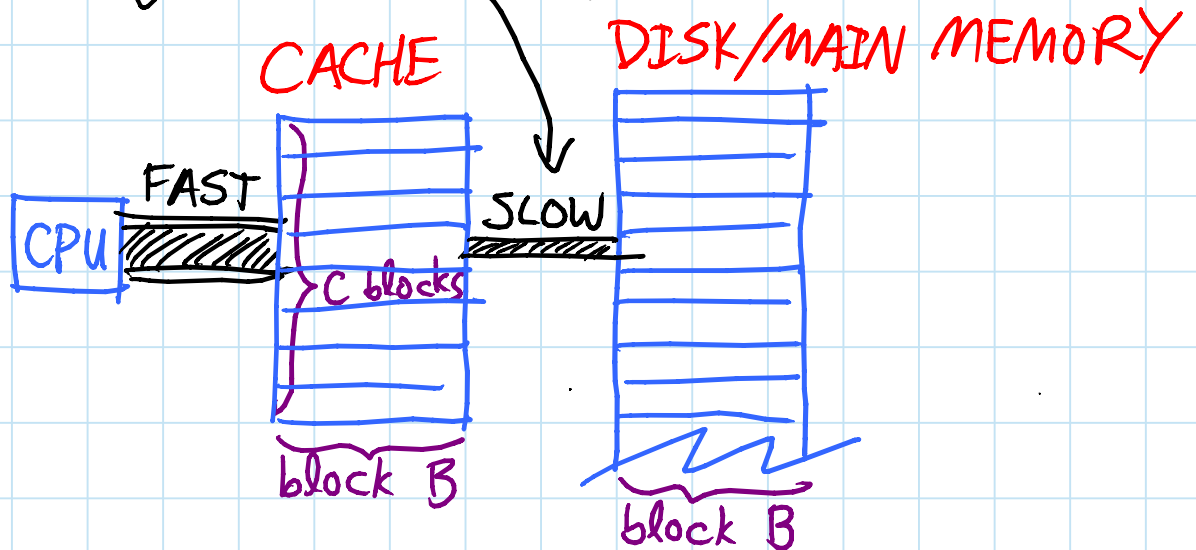
[Abel, Benbernou, Damian, Demaine, Demaine, Flatland, Kominers,  
Schweller 2010]

# Data structures: [6.851, videos next semester]

- integer data structures: store  $n$  integers in  $\{0, 1, \dots, u-1\}$  subject to insert, delete, predecessor, successor (on word RAM)
  - hashing does exact search in  $O(1)$
  - AVL trees do all in  $O(\lg n)$
  - $O(\lg \lg u)$  / op. [van Emde Boas]
  - $O(\lg n / \lg \lg u)$  / op. [fusion trees: Fredman & Willard]
  - $O(\sqrt{\lg n / \lg \lg n})$  / op. [min of above]

## - cache-efficient data structures:

- memory transfers happen in blocks



- searching takes  $\Theta(\log_B N)$  transfers (vs.  $\lg n$ )
- sorting takes  $\Theta(\frac{N}{B} \log_c \frac{N}{B})$  transfers
- possible even if you don't know  $B$  &  $C$ !

## (Almost) planar graphs: [6.889, videos online]

- Dijkstra in  $O(n)$  time  
[Henzinger, Klein, Rao, Subramanian 1997]
- Bellman-Ford in  $O(n \lg^2 n / \lg \lg n)$  time  
[Moses & Wolff-Nilson 2010]

- many problems  
NP-hard, even on  
planar graphs

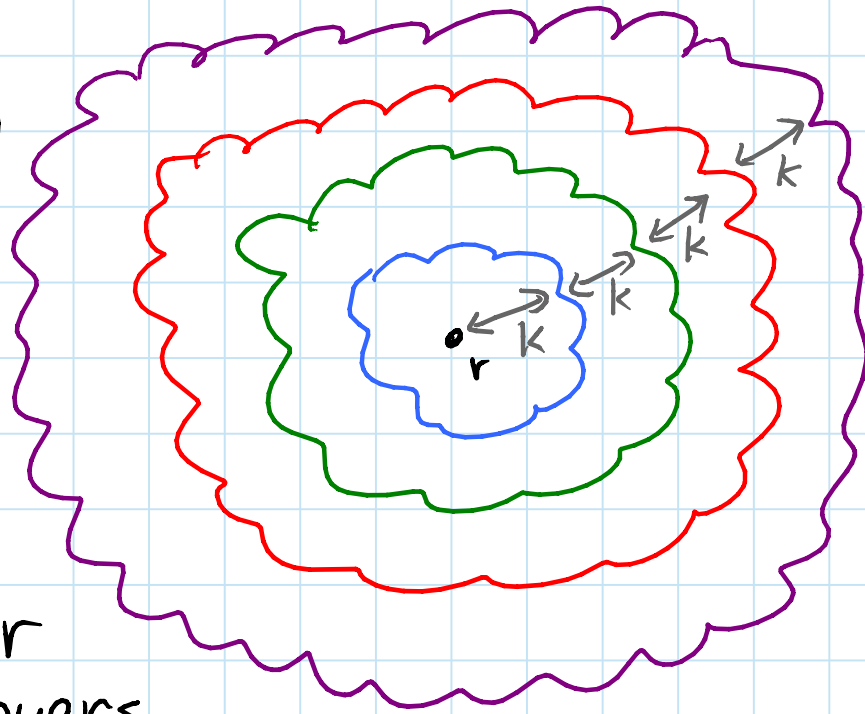
- but can find a  
solution within  
 $1+\epsilon$  factor of  
optimal, for any  $\epsilon$

- run BFS from  
any root vertex  $r$

- delete every  $k$  layers

- for many problems, solution messed up  
by only  $1 + 1/k$  factor ( $\Rightarrow k = 1/\epsilon$ )

- connected components of remaining graph  
have  $< k$  layers  $\sim$  can solve via DP  
typically in  $\sim 2^k \cdot n$  time



[Baker 1994 & others]

## Recreational algorithms:

- many algorithms & complexities of games  
[some in SP.268 & our book  
Games, Puzzles, & Computation (2009)]
- $n \times n \times n$  Rubik's Cube diameter is  $\Theta(n^2 \lg n)$   
[Demaine, Demaine, Eisenstat, Lubiw, Winslow 2011]
- Tetris is NP-complete  
[Breukelaar, Demaine, Hohenberger, Hoogeboom, Kusters, Liben-Nowell 2004]
- balloon twisting any polyhedron  
[Demaine, Demaine, Hart 2008]
- algorithmic magic tricks

## Algorithms classes at MIT: (post-6.006)

- #1: 6.046: Intermediate Algorithms  
(more adv. algorithms & analysis, less coding)
- 6.047: Computational Biology  
(genomes, phylogeny, etc.)
- 6.854: Advanced Algorithms  
(intense survey of whole field)
- 6.850: Geometric Computing  
(working with points, lines, polygons, meshes, ...)
- 6.849: Geometric Folding Algorithms  
(origami, robot arms, protein folding, ...)
- 6.851: Advanced Data Structures  
(sublogarithmic performance)
- 6.852: Distributed Algorithms  
(reaching consensus in a network with faults)
- 6.853: Algorithmic Game Theory  
(Nash equilibria, auction mechanism design, ...)
- 6.855: Network Optimization  
(optimization in graph: beyond shortest paths)
- 6.856: Randomized Algorithms  
(how randomness makes algs. simpler & faster)
- 6.857: Network and Computer Security  
(cryptography)

## Other theory classes:

- 6.045: Automata, Computability, & Complexity
- 6.840: Theory of Computing
- 6.841: Advanced Complexity Theory
- 6.842: Randomness & Computation
- 6.845: Quantum Complexity Theory
- 6.440: Essential Coding Theory
- 6.441: Information Theory

MIT OpenCourseWare  
<http://ocw.mit.edu>

6.006 Introduction to Algorithms  
Fall 2011

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